



COMPLEXITY GROWTH IN THE BIG HISTORY. A PRELIMINARY QUANTITATIVE ANALYSIS

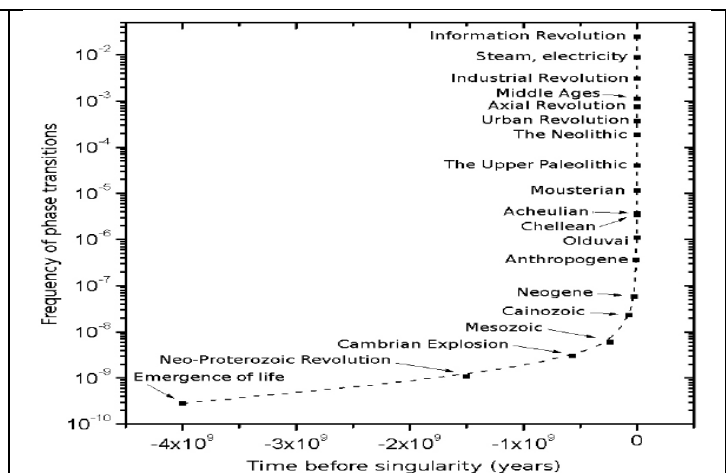
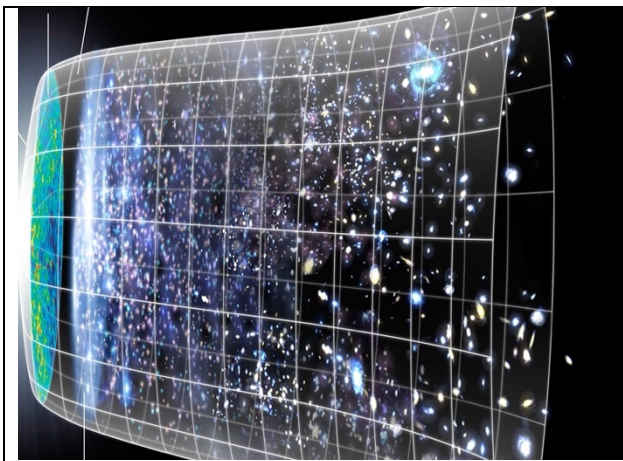
Andrey Korotayev

HSE University,

Moscow State University, and

Eurasian Center for Big History & System Forecasting at
Institute of Oriental Studies, Russian Academy of Sciences

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This presentation will be structured as follows.

In its first part, I present a summary of my previous systematic quantitative analysis of the accelerating global (biosocial) complexity growth observed for about 4 billion years on the planet Earth since the emergence of life on it and till the early 1970s.

In the second part, I apply the same methodology that I have applied to analyze this accelerating pattern to the analysis of decelerating universal (cosmic) complexity growth evidenced in the Universe for a few billions of years since the Big Bang Singularity (around 13.8 billion years BP).

Finally, the third part offers a systematic comparison of the both patterns.

44

World-Systems Evolution and Global Futures

Andrey V. Korotayev
David J. LePoire *Editors*

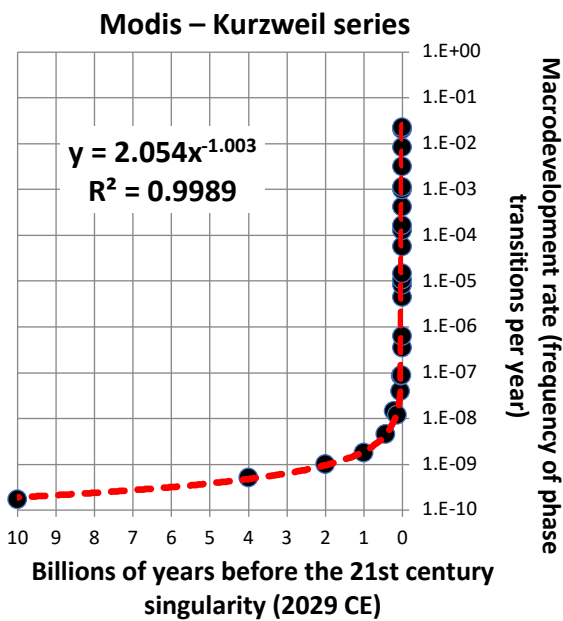
The 21st Century Singularity and Global Futures

A Big History Perspective

 Springer

As I only have 20 minutes for my presentation, it appears impossible to describe the methodology of my previous systematic quantitative analysis of the accelerating global (biosocial) evolutionary development within such a short period of time; so, I have to limit myself to the presentation of its results. A detailed description of methodology can be found in my contribution to Springer edited volume *The 21st Century Singularity and Global Futures: A Big History Perspective*, the image of whose cover can be seen to the left.

38 + 44 = 82 = 1'22

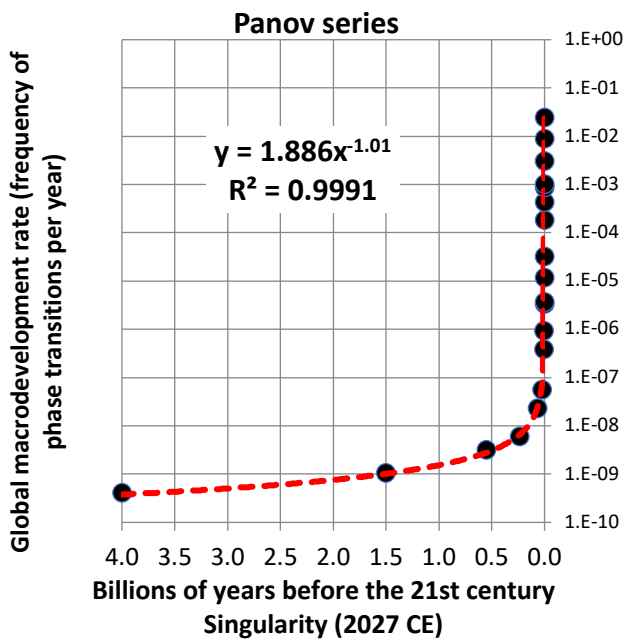


Our analysis has demonstrated that the accelerating global (biosocial) evolutionary development observed for about 4 billion years on the planet Earth since the emergence of life on it can be very accurately described by the following equation:

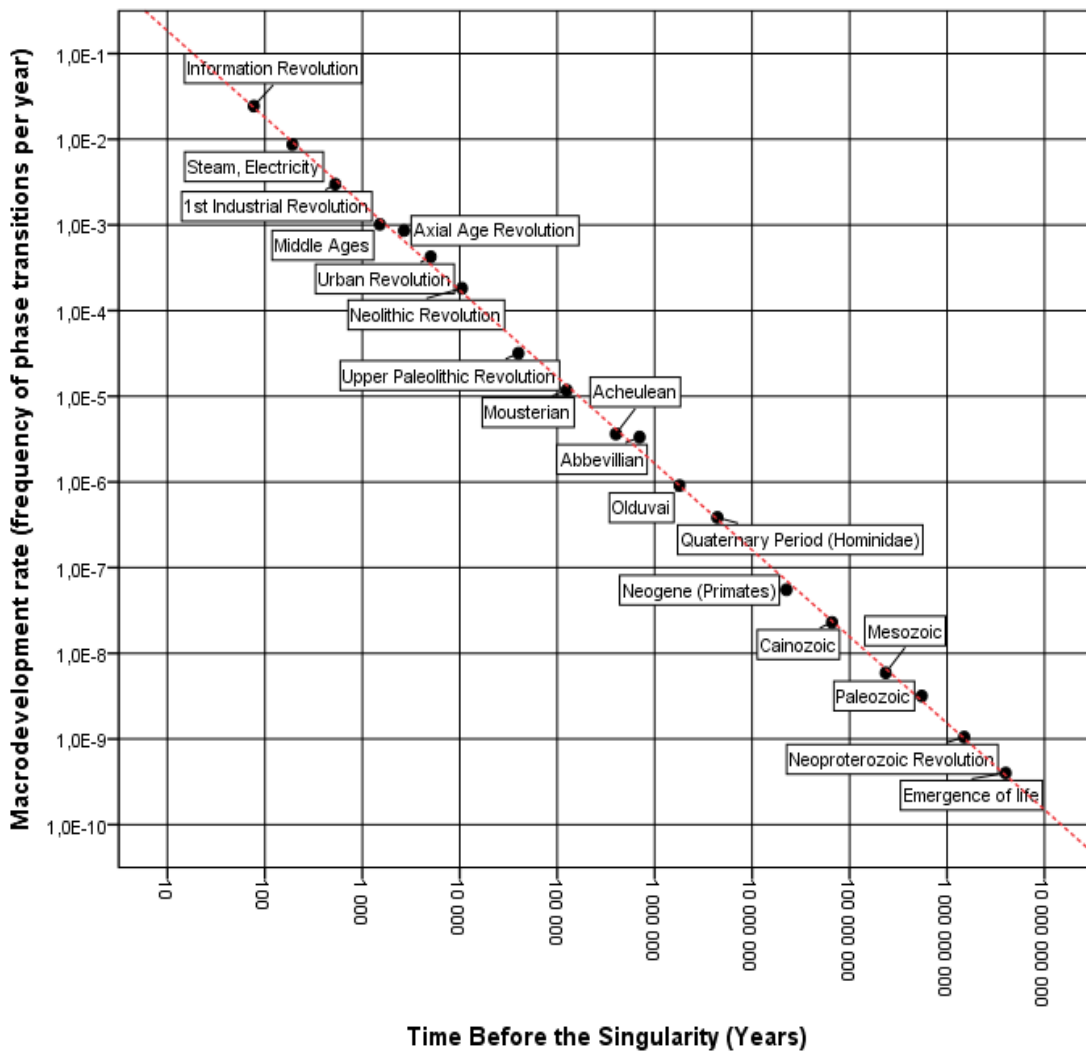
$$y_t = \frac{C}{t^* - t},$$

where y_t is the global macrodevelopment rate (complexity jumps per a unit of time) at time t , t^* is the time of singularity, and C is a constant.

The singularity time has been identified by this analysis as being around 2027–2029 CE.



38 (82 + 38 = 120 = 2')



Here you can see the fit between the theoretical curve generated by the hyperbolic equation above and the empirical estimates produced by Alexander Panov.

12 (120 + 12 = 132 = 2^7 12)

$$y = \frac{C}{t^* - t}$$

Thus, the general formula of the acceleration of the global complexity growth can be described as follows:

- The rate of the global complexity growth increases when we approach the Singularity.
- As the time till the Singularity decreases n times, the global complexity growth rate increases the same n times.
- Thus, if the time till the Singularity lessens by a factor of 3, the speed of the global complexity growth rises 3 times; if the time till the Singularity diminishes 10 times, the global complexity growth rate escalates by a factor of 10, and so on.

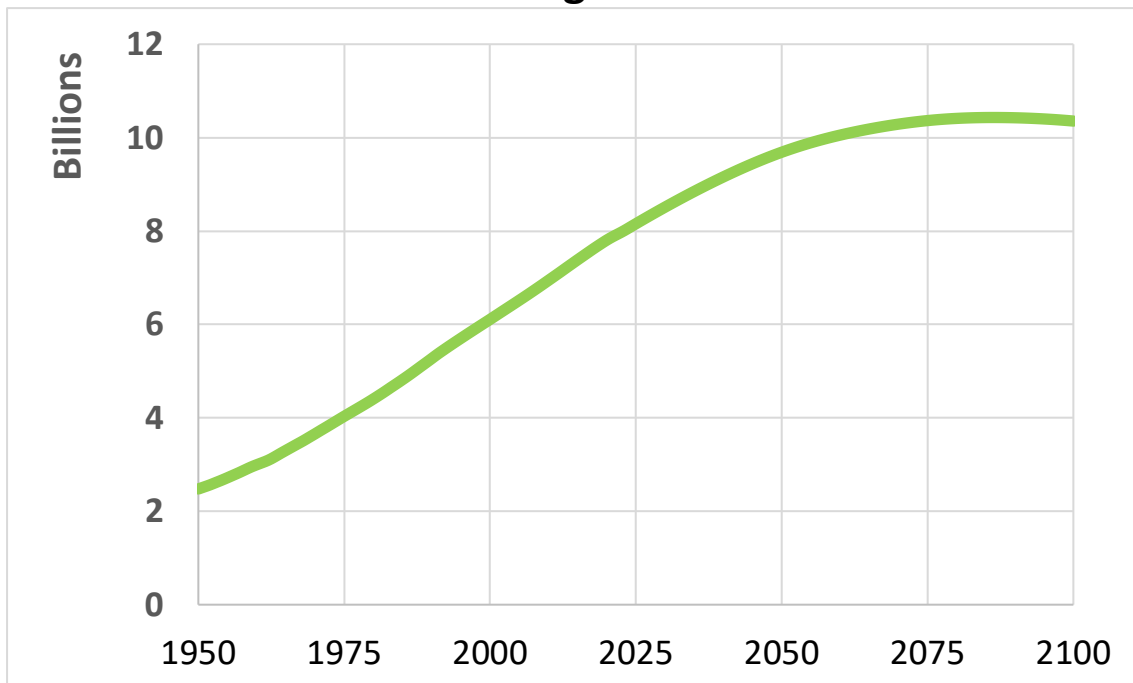
40 (132 + 40 = 172 = 2' 52)

An important disclaimer:

- How seriously should we take the prediction of “singularity” contained in such mathematical models?
- Should we really expect with Kurzweil that around 2029 we should deal with a few orders of magnitude acceleration of the technological growth (indeed, predicted by one of equations above if we take it literally)?
- I don’t think so. This is suggested, for example, by the empirical data on the world population dynamics. As we have shown earlier on quite a few occasions, the global population growth acceleration pattern discovered by Heinz von Foerster is identical with planetary macroevolutionary acceleration patterns of Modis – Kurzweil and Panov, and it is characterized by the singularity parameter (2027 CE) that is simply identical for Panov and has just 2 year difference with Modis – Kurzweil.
- However, what are the grounds to expect that by Friday, November 13, A.D. 2026 the world population growth rate will increase by a few orders of magnitude as is implied by von Foerster equation?
- The answer to this question is very clear. There are no grounds to expect this at all. Indeed, as we showed quite time ago, “von Foerster and his colleagues did not imply that the world population on [November 13, A.D. 2026] could actually become infinite. The real implication was that the world population growth pattern that was followed for many centuries prior to 1960 was about to come to an end and be transformed into a radically different pattern. Note that this prediction began to be fulfilled only in a few years after the "Doomsday" paper was published” (Korotayev 2008: 154).

118 (1073+118=1191=19* 51)

**Indeed,
starting from the early 1970s
the world population growth curve
began to diverge more and more
from the almost ideal hyperbolic shape
it had before,
and in recent decades
it has been taken more and more clearly logistic shape –
the trend towards hyperbolic acceleration
has been clearly replaced
with the logistic slow-down**



World population dynamics (billions), empirical estimates of the UN Population Division for 1950–2022 with its middle forecast till 2100

**There are all grounds to maintain
that the deceleration of planetary macroevolutionary development
has also already begun –
and it started a few decades before the singularity time points
detected both in Modis – Kurzweil and Panov.**

44 (1191+44=1235=20* 35)

The application of the same methodology
that I have applied earlier
to analyze the abovementioned accelerating
pattern
to the analysis of decelerating universal (cosmic)
evolutionary development
evidenced in the Universe for a few billions of years
since the Big Bang Singularity
has yielded the following results.

27 (172 + 27 = 199 = 3' 19)

We have used the following time series for our analysis, taking into account the following phases of the universal complexity growth:

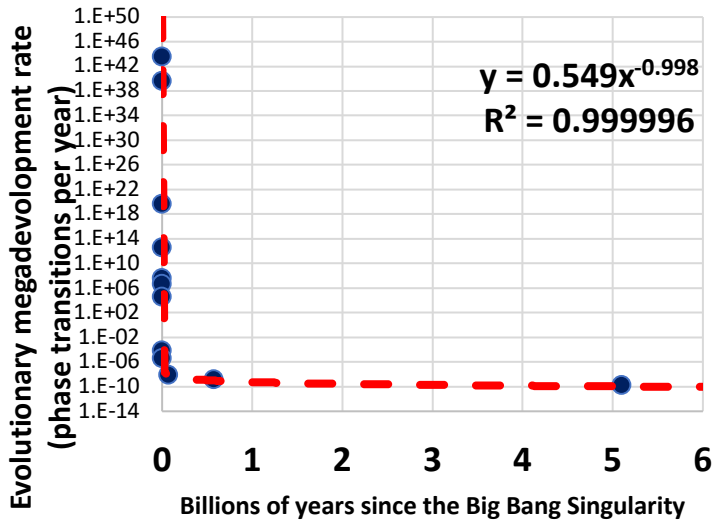
<i>Phases of the universal complexity growth</i>	<i>Seconds since the Big Bang Singularity</i>	<i>Years since the Big Bang Singularity (~13.8 billion years BP)</i>	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>
Plank epoch	before 10^{-43}	before $3.17 \cdot 10^{-51}$		
<u>Plank epoch > Grand unification epoch</u>	10^{-43}	$3.17 \cdot 10^{-51}$	$3.17 \cdot 10^{-51}$	$3.16 \cdot 10^{50}$
Grand unification epoch	from 10^{-43} to 10^{-36}	from $3.17 \cdot 10^{-51}$ to $3.17 \cdot 10^{-44}$		
<u>Grand unification epoch > Inflationary epoch</u>	10^{-36}	$3.17 \cdot 10^{-44}$	$3.17 \cdot 10^{-44}$	$3.16 \cdot 10^{43}$
Inflationary epoch	from 10^{-36} to 10^{-32}	from $3.17 \cdot 10^{-44}$ to $3.17 \cdot 10^{-40}$		
<u>Inflationary epoch > Electroweak epoch</u>	10^{-32}	$3.17 \cdot 10^{-40}$	$3.17 \cdot 10^{-40}$	$3.16 \cdot 10^{39}$
Electroweak epoch	from 10^{-32} to 10^{-12}	from $3.17 \cdot 10^{-40}$ to $3.17 \cdot 10^{-20}$		
<u>Electroweak epoch > Quark epoch</u>	10^{-12} (one trillionth of a second)	$3.17 \cdot 10^{-20}$	$3.17 \cdot 10^{-20}$	$3.16 \cdot 10^{19}$
Quark epoch	from 10^{-12} to 10^{-5}	from $3.17 \cdot 10^{-20}$ to $3.17 \cdot 10^{-13}$		
<u>Quark epoch > Hadron epoch</u>	10^{-5} (0.00001, 10 millionths of a second)	$3.17 \cdot 10^{-13}$	$3.17 \cdot 10^{-13}$ of a year (~1 millionth of a second)	$3.16 \cdot 10^{12}$ (3.16 trillion phase transitions per year)
Hadron epoch	from 10^{-5} to 1 second since the Big Bang Singularity	from $3.17 \cdot 10^{-13}$ to $3.17 \cdot 10^{-8}$		
<u>Hadron epoch > Lepton epoch</u>	1 second since the Big Bang Singularity (= after Singularity / AS)	$3.17 \cdot 10^{-8}$	$3.17 \cdot 10^{-8}$ of a year (~1 second)	$3.16 \cdot 10^7$ (31.6 million phase transitions per year)

<i>Phases of the universal complexity growth</i>	Seconds since the Big Bang Singularity	Years since the Big Bang Singularity (~13.8 billion years BP)	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>
Lepton epoch, Neutrino decoupling	from 1 to 10 seconds since the Big Bang Singularity / AS	from $3.17 \cdot 10^{-8}$ to $3.17 \cdot 10^{-7}$		
<u>Lepton epoch > Big Bang nucleosynthesis</u>	<u>10 seconds</u>	<u>$3.17 \cdot 10^{-7}$</u>	$2.87 \cdot 10^{-7}$ of a year (~9 seconds)	$3.51 \cdot 10^6$ (3.51 million phase transitions per year)
Big Bang nucleosynthesis	from 10 to 1000 seconds AS	from $3.17 \cdot 10^{-7}$ to $3.17 \cdot 10^{-5}$		
<u>Big Bang nucleosynthesis > Photon epoch</u>	<u>1000 seconds</u>	<u>$3.17 \cdot 10^{-5}$</u>	$3.14 \cdot 10^{-5}$	$3.19 \cdot 10^4$ (31,900 phase transitions per year)
Photon epoch	from 1000 seconds	to 18 thousand years AS		
<u>Photon epoch > Recombination</u>	<u>$5.68 \cdot 10^{11}$</u>	<u>$1.8 \cdot 10^4$ (18 thousand years)</u>	$1.8 \cdot 10^4$ (18 thousand years)	$5.56 \cdot 10^{-5}$ (5.56 phase transitions per 100 thousand years)
Recombination	from $5.68 \cdot 10^{11}$ to $1.17 \cdot 10^{13}$	from 18 thousand to 370 thousand years AS		
<u>Recombination > Dark ages</u>	<u>$1.17 \cdot 10^{13}$</u>	<u>370 thousand years since the B. Bang Singularity</u>	$3.52 \cdot 10^5$ (352 thousand years)	$2.84 \cdot 10^{-6}$ (2.28 phase transitions per 1 million years)
Dark ages mid-phase	from $1.17 \cdot 10^{13}$ to $4.73 \cdot 10^{15}$	from 370 thousand to 150 million years AS		
<u>Dark ages > Population III stars</u>	<u>$4.73 \cdot 10^{15}$</u>	<u>150 million (13.625 billion years BP)</u>	$1.496 \cdot 10^8$ (149.63 million years)	$6.68 \cdot 10^{-9}$ (6.68 phase transitions per 1 billion years)

<i>Phases of the universal complexity growth</i>	Seconds since the Big Bang Singularity	Years since the Big Bang Singularity (~13.8 billion years BP)	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>
Population III stars, earliest galaxies, reionization , mid-phase	from $4.73 \cdot 10^{15}$ to $3.16 \cdot 10^{16}$	from 150 million to 1 billion years AS		
<u>Population III stars > 2nd generation of stars</u>	<u>$3.16 \cdot 10^{16}$</u>	<u>1 billion (12 billion years BP)</u>	$8.5 \cdot 10^8$ (850 million years)	$1.18 \cdot 10^{-9}$ (1.18 phase transitions per 1 billion years)
First 3rd generation stars appear against the background of predominance of the 2nd generation of stars, medium complexity galaxies, primitive planets, primitive chemical evolution , mid-phase	from $3.16 \cdot 10^{16}$ to $2.90 \cdot 10^{17}$	from 1 billion to 9.2 billion years AS		
<u>Predominance of the 2nd population of stars > predominance of the 3rd generation of stars</u>	<u>$2.90 \cdot 10^{17}$</u>	<u>9.2 billion AS (4.6 billion years BP)</u>	$8.20 \cdot 10^9$ $8.2 \cdot 10^9$ (8.2 billion years)	$1.22 \cdot 10^{-10}$ (1.22 phase transitions per 10 billion years)
Predominance of the 3rd generation of stars, complex galaxies, complex planets, complex chemical evolution	After $2.90 \cdot 10^{17}$	After 9.2 billion AS (after 4.6 billion years BP)		

140 (199 + 140 = 239 = 3⁵ 59)

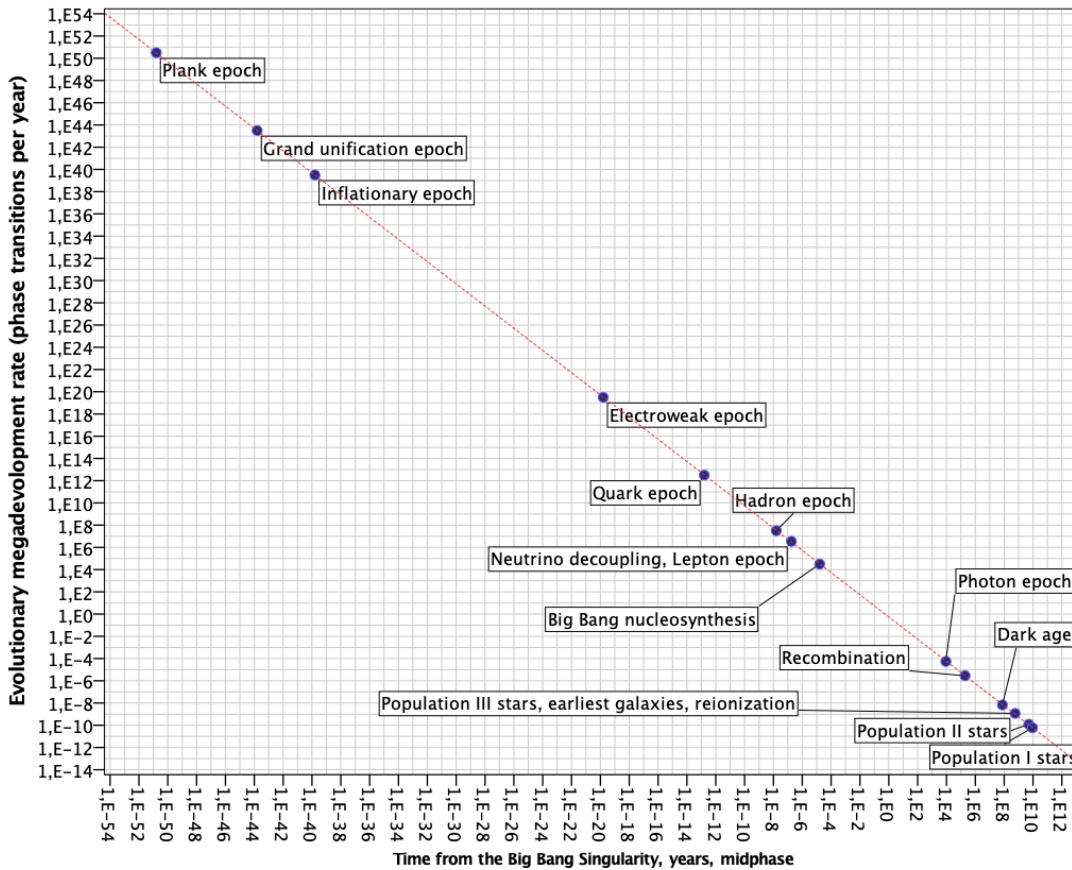
Post-Big Bang Sequence



Our analysis has demonstrated that the decelerating universal (cosmic) evolutionary development evidenced in the Universe for a few billions of years since the Big Bang Singularity can be very accurately described by the following equation:

$$y_t = \frac{C_2}{t - t^*}$$

where y_t is the rate of the universal complexity growth (complexity jumps per a unite of time) at time t ; t^* is the time of the Bing Bang singularity, and C_2 is a constant.



34 (239 + 34 = 273 = 4^33)

Decelerating universal (cosmic) evolutionary development	Accelerating global (biosocial) evolutionary development
$y = \frac{0.55}{t - t^*}$	$y = \frac{1.89}{t^* - t}$
$y = \frac{C_1}{t - t^*}$	$y = \frac{C_2}{t^* - t}$
<p>Thus, the general formula of the deceleration of the universal (cosmic) complexity growth can be described as follows:</p> <ul style="list-style-type: none"> • The rate of the universal (cosmic) complexity growth decreases when we move from the Singularity. • As the time since the Singularity increases n times, the universal (cosmic) complexity growth rate decreases the same n times. • Thus, if the time since the Singularity rises by a factor of 3, the speed of the universal (cosmic) complexity growth lessens 3 times; if the time since the Singularity increases 10 times, the universal (cosmic) complexity growth rate diminishes by a factor of 10, and so on. 	<p>Whereas, the general formula of the acceleration of the global (biosocial) complexity growth can be described as follows:</p> <ul style="list-style-type: none"> • The rate of the global complexity growth increases when we approach the Singularity. • As the time till the Singularity decreases n times, the global complexity growth rate increases the same n times. • Thus, if the time till the Singularity lessens by a factor of 3, the speed of the global complexity growth rises 3 times; if the time till the Singularity diminishes 10 times, the global complexity growth rate escalates by a factor of 10, and so on.
<p>It is difficult not to see here a striking symmetry – the basic regularities of the hyperbolic deceleration of the post-Big Bang universal increase in complexity turn out to be strikingly similar to the ones of the hyperbolic acceleration of the complexity growth observed on our planet for 4 billion years until the early 1970s.</p>	

64 (273 + 97 = 360 = 6')

**Consider now the relationship
between the radiation energy of the Universe
and universal complexity growth rate
(measured in phase transitions per year).**

10 (10 + 360 = 370 = 5' 10)

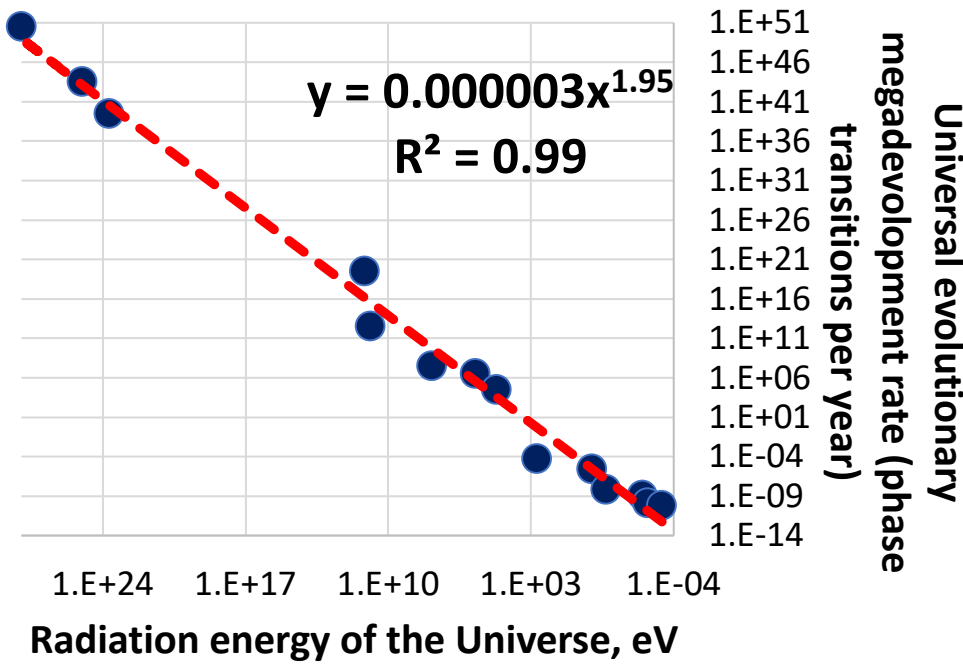
We have used the following time series for our analysis, taking into account the following phases of the universal complexity growth and corresponding values of the radiation energy of the Universe (measured in eV):

<i>Phases of the universal complexity growth</i>	<i>t – t* (seconds since the Big Bang Singularity)</i>	<i>t – t* (years since the Big Bang Singularity)</i>	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>	<i>Radiation energy of the Universe, in electronvolts (eV)</i>	<i>Radiation energy of the Universe, in Kelvins (K)</i>
<u>Plank epoch starts</u>	<u>10^{-47}</u>	<u>$3.17 \cdot 10^{-55}$</u>				
Plank epoch mid-phase	$5 \cdot 10^{-44}$	$1.58 \cdot 10^{-51}$	$3.17 \cdot 10^{-51}$	$3.16 \cdot 10^{50}$	10^{28}	$1.16 \cdot 10^{32}$
<u>Plank epoch > Grand unification epoch</u>	<u>10^{-43}</u>	<u>$3.17 \cdot 10^{-51}$</u>				
Grand unification epoch mid-phase	$5 \cdot 10^{-37}$	$1.58 \cdot 10^{-44}$	$3.17 \cdot 10^{-44}$	$3.16 \cdot 10^{43}$	10^{25}	$1.16 \cdot 10^{29}$
<u>Grand unification epoch > Inflationary epoch</u>	<u>10^{-36}</u>	<u>$3.17 \cdot 10^{-44}$</u>				
Inflationary epoch mid-phase	$5 \cdot 10^{-33}$	$1.58 \cdot 10^{-40}$	$3.17 \cdot 10^{-40}$	$3.16 \cdot 10^{39}$	$5 \cdot 10^{23}$	$5.8 \cdot 10^{27}$
<u>Inflationary epoch > Electroweak epoch</u>	<u>10^{-32}</u>	<u>$3.17 \cdot 10^{-40}$</u>				
Electroweak epoch mid-phase	$5 \cdot 10^{-13}$	$1.58 \cdot 10^{-20}$	$3.17 \cdot 10^{-20}$	$3.16 \cdot 10^{19}$	150 billion eV (150 GeV)	$1.74 \cdot 10^{15}$
<u>Electroweak epoch > Quark epoch</u>	<u>10^{-12} (one trillionth of a second)</u>	<u>$3.17 \cdot 10^{-20}$</u>				
Quark epoch mid-phase	$5 \cdot 10^{-06}$	$1.58 \cdot 10^{-13}$	$3.17 \cdot 10^{-13}$ of a year (~1 millionth of a second)	$3.16 \cdot 10^{12}$ (3.16 trillion phase transitions per year)	75.1 billion eV (75.1 GeV)	$8.71 \cdot 10^{14}$ (871 trillion K)
<u>Quark epoch > Hadron epoch</u>	<u>10^{-05} (0.00001, 10 millionths of a second)</u>	<u>$3.17 \cdot 10^{-13}$</u>				
Hadron epoch mid-phase	0.500005	$1.58 \cdot 10^{-8}$	$3.17 \cdot 10^{-8}$ of a year (~1 second)	$3.16 \cdot 10^7$ (31.6 million phase transitions per year)	75.5 million eV (75.5 MeV)	$8.76 \cdot 10^{11}$ (876 billion K)

<i>Phases of the universal complexity growth</i>	$t - t^*$ (seconds since the Big Bang Singularity)	$t - t^*$ (years since the Big Bang Singularity)	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>	Radiation energy of the Universe, in electronvolts (eV)	Radiation energy of the Universe, in Kelvins (K)
<u>Hadron epoch > Lepton epoch</u>	<u>1 second since the Big Bang Singularity</u>	<u>$3.17 \cdot 10^{-8}$</u>				
Lepton epoch, Neutrino decoupling, mid-phase	5.5 seconds	$1.74 \cdot 10^{-7}$	$2.87 \cdot 10^{-7}$ of a year (~9 seconds)	$3.51 \cdot 10^6$ (3.51 million phase transitions per year)	550,000 (550 KeV)	$6.38 \cdot 10^9$ (6.38 billion K)
<u>Lepton epoch > Big Bang nucleosynthesis</u>	<u>10 seconds</u>	<u>$3.17 \cdot 10^{-7}$</u>				
Big Bang nucleosynthesis mid-phase	505 seconds	$1.60 \cdot 10^{-5}$	$3.14 \cdot 10^{-5}$	$3.19 \cdot 10^4$ (31,900 phase transitions per year)	50,500 (50.5 KeV)	$5.86 \cdot 10^8$ (586 million K)
<u>Big Bang nucleosynthesis > Photon epoch</u>	<u>1000 seconds</u>	<u>$3.17 \cdot 10^{-5}$</u>				
Photon epoch mid-phase	$2.84 \cdot 10^{11}$	$9.0 \cdot 10^3$ (9 thousand years since the B. Bang Singularity)	$1.8 \cdot 10^4$ (18 thousand years)	$5.56 \cdot 10^{-5}$ (5.56 phase transitions per 100 thousand years)	500 eV	$5.86 \cdot 10^6$ (5.86 million K)
<u>Photon epoch > Recombination</u>	<u>$5.68 \cdot 10^{11}$</u>	<u>$1.8 \cdot 10^4$ (18 thousand years)</u>				
Recombination mid-phase	$6.12 \cdot 10^{12}$	194 thousand years AS	$3.52 \cdot 10^5$ (352 thousand years)	$2.84 \cdot 10^{-6}$ (2.28 phase transitions per 1 million years)	1 eV	$1.16 \cdot 10^4$ (11.6 thousand K)
<u>Recombination > Dark ages</u>	<u>$1.17 \cdot 10^{13}$</u>	<u>370 thousand years since the B. Bang Singularity</u>				
Dark ages mid-phase	$2.37 \cdot 10^{15}$	75.2 million (13.7 billion years BP)	$1.496 \cdot 10^8$ (149.63 million years)	$6.68 \cdot 10^{-9}$ (6.68 phase transitions per 1 billion years)	0.203 eV	2,350 K
<u>Dark ages > Population III stars</u>	<u>$4.73 \cdot 10^{15}$</u>	<u>150 million (13.625 billion years BP)</u>				
Population III stars, earliest galaxies, reionization, mid-phase	$1.81 \cdot 10^{16}$	575 million (13.2 billion years BP)	$8.5 \cdot 10^8$ (850 million years)	$1.18 \cdot 10^{-9}$ (1.18 phase transitions per 1 billion years)	0.0034 eV	39.5 K
<u>Population III stars > 2nd generation of stars</u>	<u>$3.16 \cdot 10^{16}$</u>	<u>1 billion (12 billion years BP)</u>				

<i>Phases of the universal complexity growth</i>	$t - t^*$ (seconds since the Big Bang Singularity)	$t - t^*$ (years since the Big Bang Singularity)	<i>Time between phases (years)</i>	<i>Universal evolutionary megadevelopment rate (phase transitions per year)</i>	Radiation energy of the Universe, in electronvolts (eV)	Radiation energy of the Universe, in Kelvins (K)
First 3 rd generation stars appear against the background of predominance of the 2 nd generation of stars, medium complexity galaxies, primitive planets, primitive chemical evolution, mid-phase	$1.61 \cdot 10^{17}$	5.1 billion (8,7 billion years BP)	8.20E+09 $8.2 \cdot 10^9$ (8.2 billion years)	$1.22 \cdot 10^{-10}$ (1.22 phase transitions per 10 billion years)	$1.89 \cdot 10^3$ eV	22 K
<u>Predominance of the 2nd population of stars > predominance of the 3rd generation of stars</u>	<u>$2.90 \cdot 10^{17}$</u>	<u>9.2 billion (4.6 billion years BP)</u>				
Predominance of the 3 rd generation of stars, complex galaxies, complex planets, complex chemical evolution	After $2.90 \cdot 10^{17}$	After 9.2 billion years AS (after 4.6 billion years BP)	?	?	$3.79 \cdot 10^{-4}$ eV	4.4 K

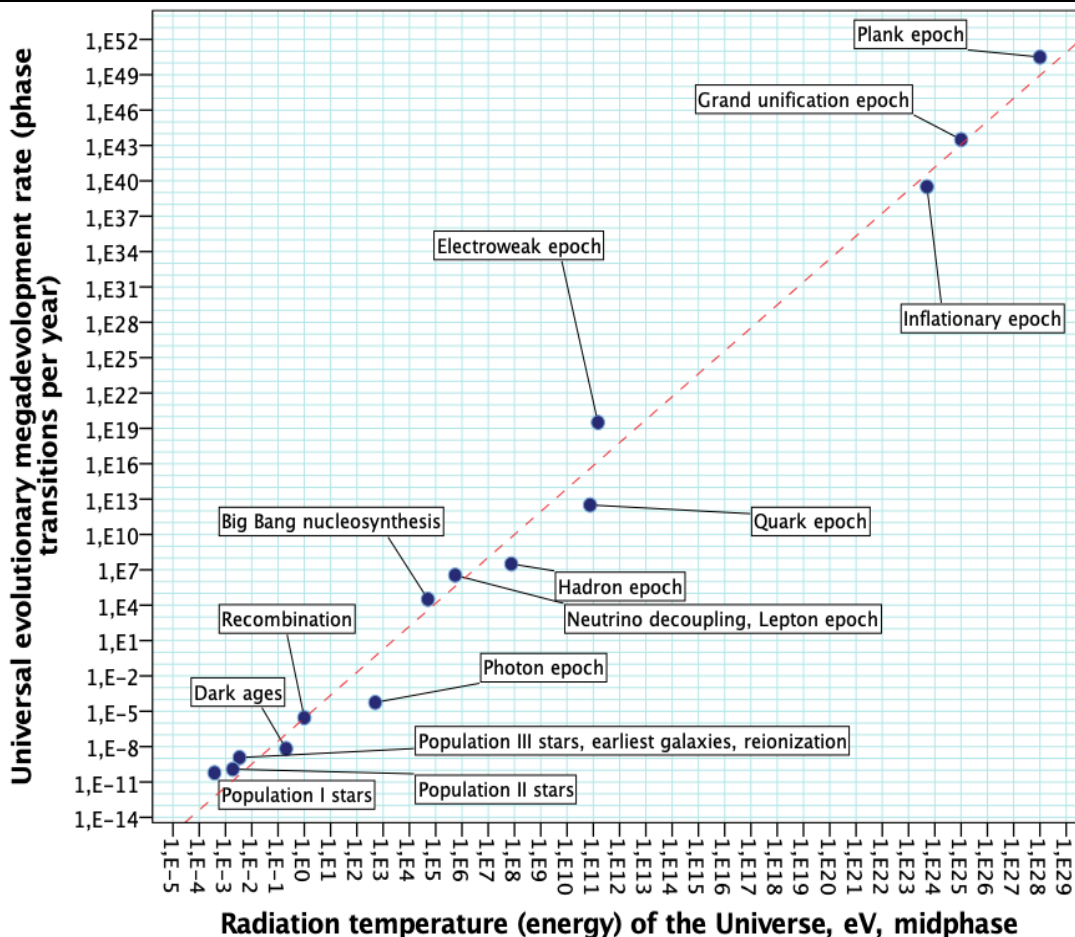
55 (370 + 55 = 425 = 7* 5)



Our analysis has demonstrated that the relationship between the radiation energy of the Universe and universal complexity growth rate can be very accurately described by the following equation:

$$y = C_4 * E^2$$

where y is the rate of the universal complexity growth (complexity jumps per a unit of time); E is the radiation energy of the Universe (eV), and C_4 is a constant.



27 (425 + 27 = 452 = 7³ 32)

$$y = C_4 * E^2$$

Thus, in the cosmic history
the rate of the universal complexity growth
was proportional to the radiation energy
of the Universe squared.

10 (452 + 10 = 462 = 7' 42)

It can be easily shown analytically that if within the cosmic evolution the rate of the universal complexity growth y equals constant C_1 divided by the time since the Big Bang Singularity ($t - t^*$, or x)

$$y = \frac{C_1}{t - t^*}$$

and the rate of the universal complexity growth y is proportional to the radiation energy of the Universe E squared

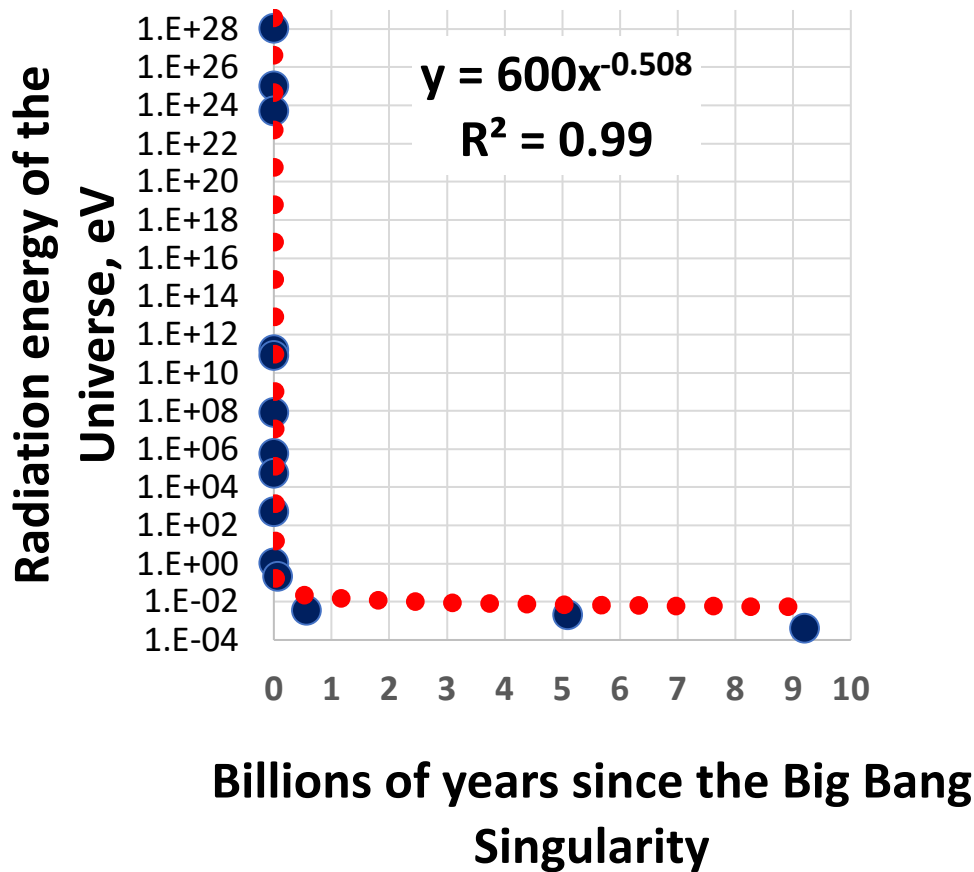
$$y = C_4 * E^2$$

then the radiation energy of the Universe E should be proportional to some constant $C_3 (= C_1/C_4)$ divided by a square root of the time since the Big Bang Singularity ($t - t^*$, or x)

$$E = \frac{C_3}{\sqrt{t-t^*}} = C_3 x^{-0.5} = C_3 x^{-\frac{1}{2}}$$

$y = \frac{C_1}{t-t^*}$	$y = C_4 * E^2$
$C_4 * E^2 = \frac{C_1}{t-t^*}$	
$E^2 = \frac{C_1}{C_4} \frac{1}{t-t^*}$	
$E^2 = \frac{C_3}{t-t^*}$, where $C_3 = \frac{C_1}{C_4}$	
$E = \frac{C_3}{\sqrt{t-t^*}} = C_3 x^{-0.5}$	

27 (462 + 27 = 489 = 8' 9)

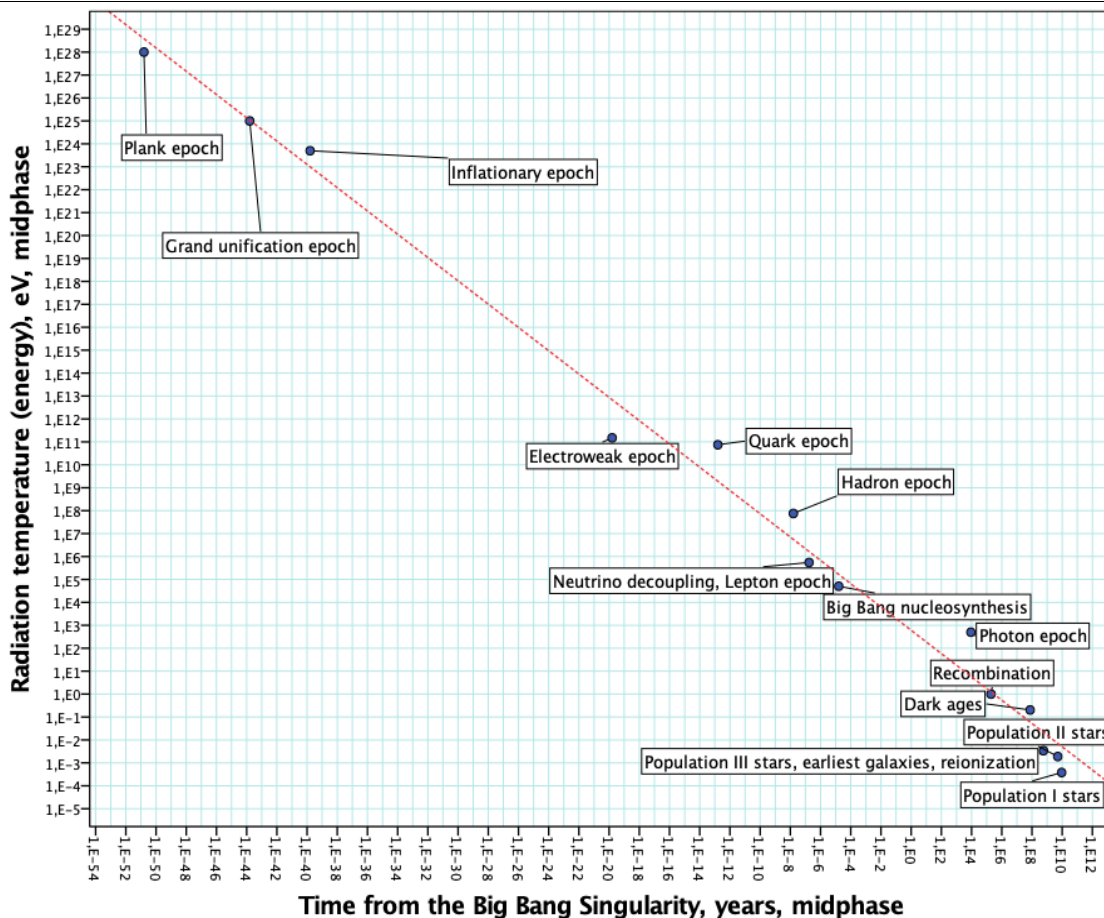


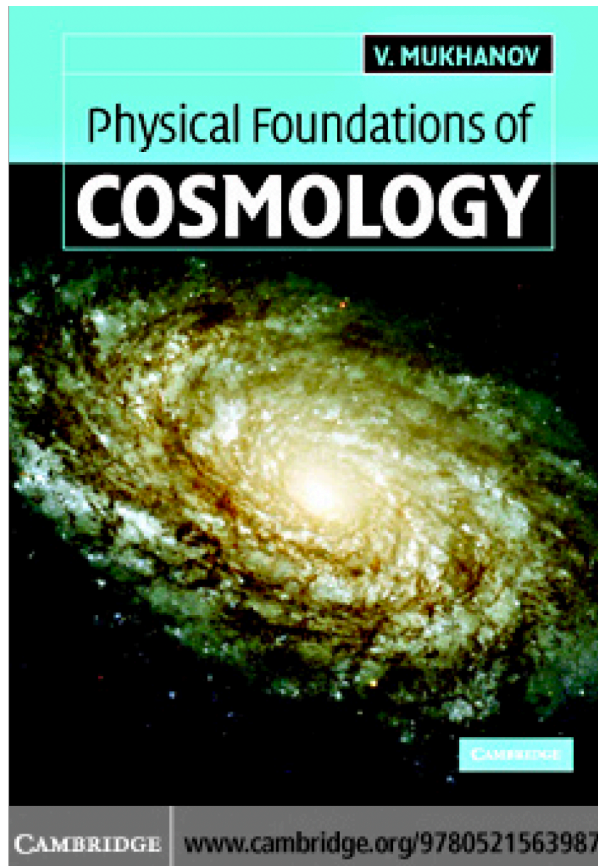
The analysis of the data presented above suggests that this is indeed the case. Our analysis has demonstrated that the relationship between time since the Big Bang Singularity (years) and radiation energy of the Universe (eV) can be quite accurately described by the following equation:

$$E = \frac{C_3}{\sqrt{t - t^*}}$$

or

$E = C_3 x^{-0.5}$
where E is the radiation energy of the Universe (eV); x (or $t - t^*$) is the time since the Big Bang Singularity, and C_3 is a constant.





Problem 3.3 Dark energy with equation of state $w = -1/3$ leads to a term $\propto 1/a^2$ in the Friedmann equation (1.67). How can we nevertheless distinguish it from the spatial curvature term, k/a^2 , in an open universe?

3.2 Brief thermal history

The temperature of the cosmic radiation decreases as the universe expands. It is unambiguously related to the redshift,

$$T_\gamma(z) = T_{\gamma 0}(1 + z), \quad (3.4)$$

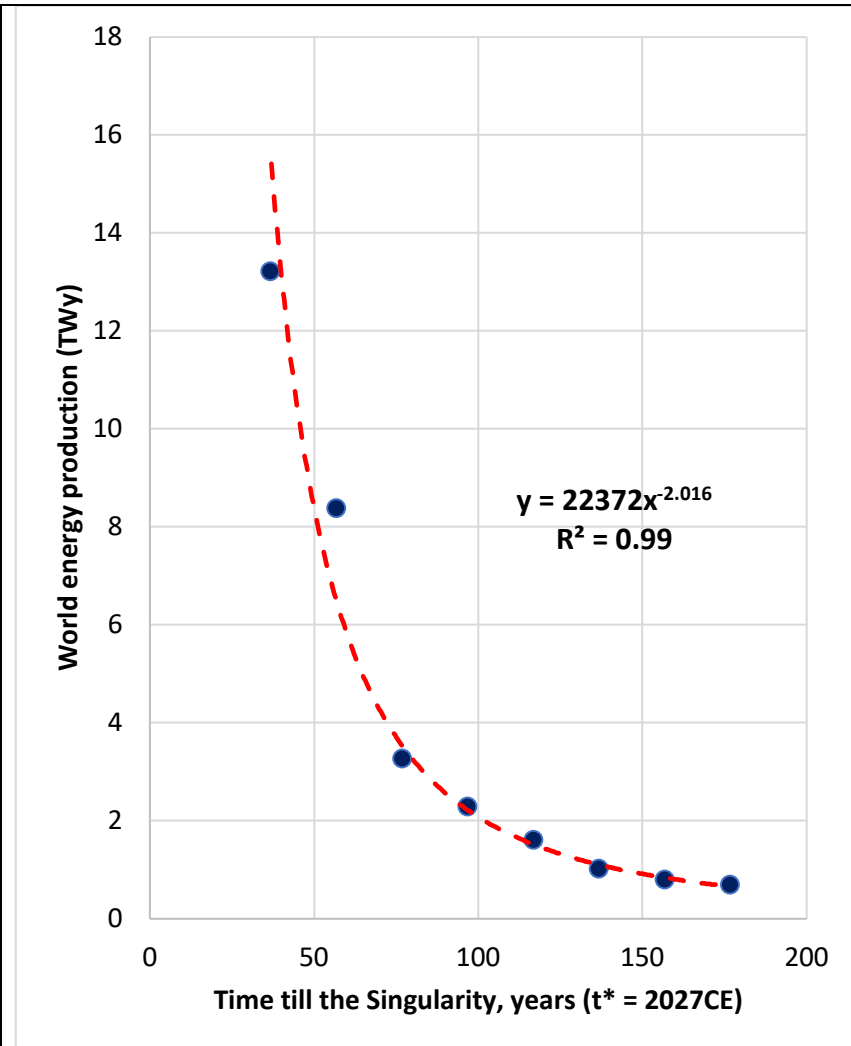
and can be used as an alternative to time or redshift to parameterize the history of the universe. To obtain an estimate for the temperature expressed in MeV, at the time t measured in seconds, we can use the formula

$$T_{\text{MeV}} \simeq \frac{O(1)}{\sqrt{t_{\text{sec}}}},$$

In fact, this relationship is well known in cosmology and may be derived from original Friedman's equations.

This suggests that the post-Big Bang hyperbolic deceleration of the universal complexity growth was directly connected with the post-Big Bang hyperbolic deceleration of the cooling of the Universe described by the equation below

$$E = \frac{C_3}{\sqrt{t - t^*}}$$



Consider now the relationship between time till the 21st century singularity (years) and world energy production (TWy) estimated by John Holdren.

As we see, for the pattern of global hyperbolic acceleration we find a quadratic relationship between the energy production and the time till the singularity inversed to the one we saw with respect to the post-Big-Bang universal deceleration

$$E = \frac{C_6}{(t^* - t)^2}$$

Correspondingly the relationship between world energy production (E , TWy) and global (biosocial) evolutionary megadevelopment rate (y , phase transitions per year) is described by the following equation

$$y = C_5 \sqrt{E}$$

11 (566 + 11 = 577 = 9' 37)

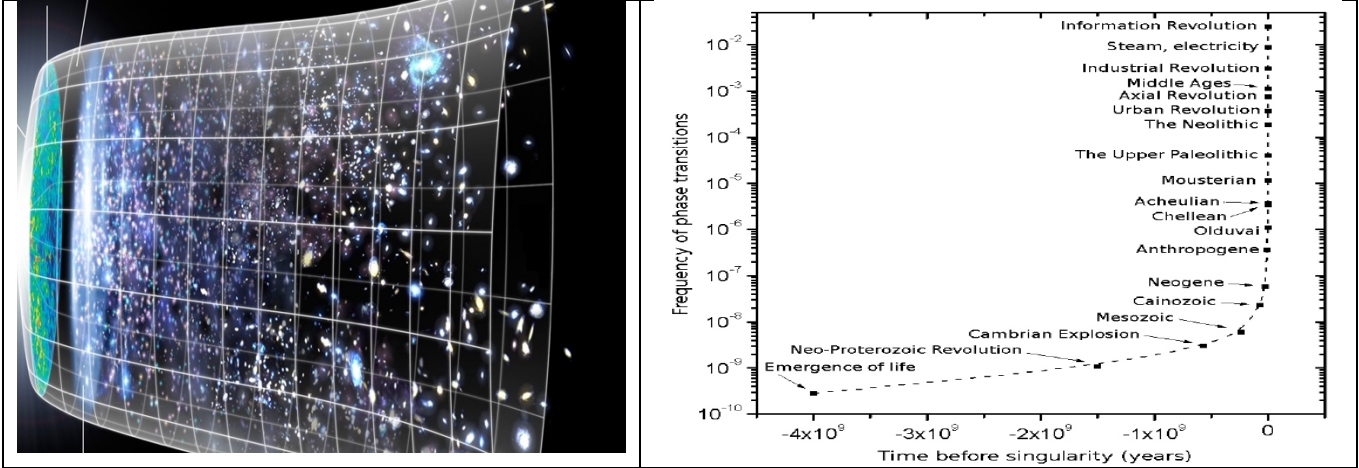
Decelerating universal (cosmic) evolutionary development		Accelerating global (biosocial) evolutionary development		Thus, the correlations between energy and decelerating growth of universal complexity display a striking symmetry with inversions in comparison with accelerating global evolutionary development.
Relationship between time since the Big Bang Singularity ($t-t^*$, years) and universal evolutionary megadevelopment rate (y , phase transitions per year)	$y = \frac{C_1}{t - t^*}$	Relationship between time till the 21 st century singularity (t^*-t , years) and global (biosocial) evolutionary megadevelopment rate (y , phase transitions per year)	$y = \frac{C_2}{t^* - t}$	
Relationship between radiation temperature (energy) of the Universe (E , eV) and universal evolutionary mega-development rate (y , phase transitions per year)	$y = C_4 * E^2$	Relationship between world energy production (E , TWy) and global (biosocial) evolutionary mega-development rate (y , phase transitions per year)	$y = C_5 \sqrt{E}$	<p>In the cosmic history the rate of the universal complexity growth was proportional to the radiation energy of the Universe squared.</p> <p>In the global history the rate of the global complexity growth was proportional to the square root of the world energy production.</p>

<p>Relationship between time since the Big Bang Singularity ($t-t^*$, years) and radiation energy of the Universe (E, eV)</p>	$E = \frac{C_3}{\sqrt{t - t^*}}$	<p>Relationship between time till the 21st century singularity (t^*-t, years) and world energy production (E, TWy)</p>	$E = \frac{C_6}{(t^*-t)^2}$	<p>In the cosmic history the moving from the Big Bang Singularity by n times was accompanied by the decrease of the radiation energy of the Universe by \sqrt{n} times. Thus, the increase in the time since the Singularity by a factor of 4 was associated with the drop in the radiation energy of the Universe by a factor of 2.</p>
<p>On the other hand, in the global history the moving toward the 21st century singularity by n times was associated with growth of the world energy production by n^2 times. Thus, the decrease in the time till the singularity by a factor of 4 was associated with the increase in the world energy production by a factor of 16.</p>				

80 (577 + 80 = 657 = 10² · 57)

Of course, this presentation poses more questions than it answers. The most important of those questions seems to be – why do the basic regularities of the hyperbolic deceleration of the post-Big Bang universal increase in complexity turn out to be so strikingly similar to the ones of the global hyperbolic acceleration of the complexity growth when their mechanisms are so different?

$$24(657 + 24 = 681 = 11'21)$$



World-Systems Evolution and Global Futures

Andrey V. Korotayev
David J. LePoire *Editors*

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On the one hand, it has been shown that the global hyperbolic acceleration pattern of the last 4 billion years appears to have been produced endogenously by the second order positive feedback between the complexity of the global sociobiological system and the rate of its complexity growth:

the more complex the global biosocial system, the less time it takes it to make the next complexity jump.

It has been shown that when written mathematically, such a feedback produces precisely a hyperbolic acceleration effect.

38 + 44 = 82 = 1 * 22

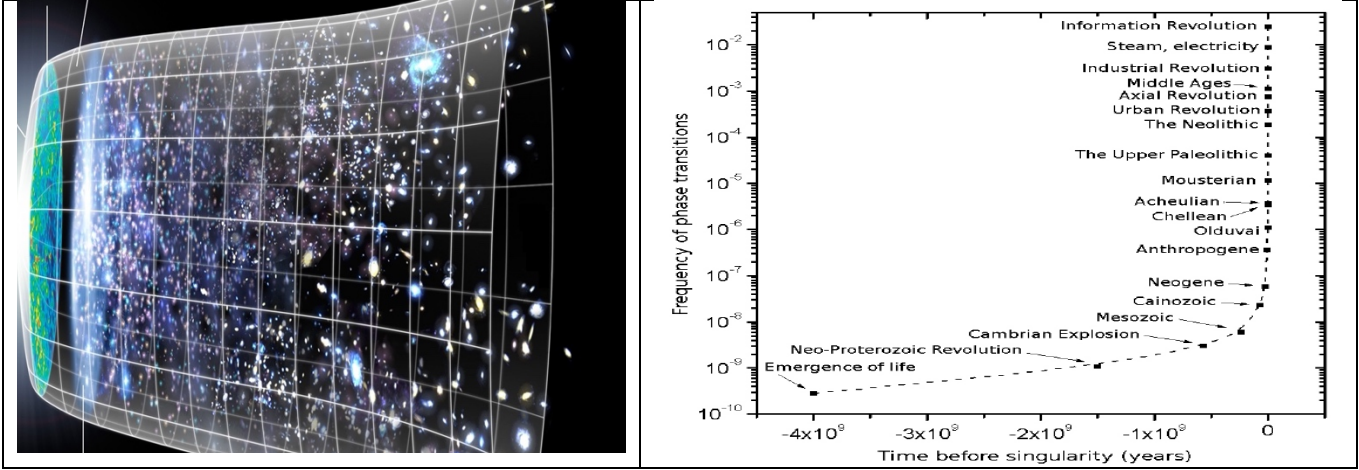
On the other hand, the hyperbolic deceleration of the post-Big-Bang of the universal complexity growth rate appears to have been produced exogenously by the post-Big-Bang hyperbolic deceleration of the cooling of the Universe: the slower this cooling proceeded, the slower the universal complexity grew – thus, the post-Big-Bang hyperbolic deceleration of the cooling of the Universe resulted in the hyperbolic deceleration of the post-Big-Bang deceleration of the universal complexity growth rate.

After the Big Bang Singularity, the growth of complexity in the Universe was very tightly connected with its cooling. It was this cooling that allowed the formation in the Universe of more and more complex entities – quarks, then hadrons, then atomic nuclei, then atoms, then molecules.

At the very beginning the cooling of the Universe proceeded very fast, and the complexity in the Universe grew extremely fast (with a few phase transitions just within the first second after the Big Bang Singularity). Then the cooling of the Universe slowed down, which caused the slowing down of the growth of complexity in the Universe.

As we have seen, the slowing down of the cooling of the Universe followed a hyperbolic pattern, and it does not appear to be of any surprise that the hyperbolic slowdown of the cooling of the Universe after the Big Bang Singularity caused a hyperbolic slowdown of the universal complexity growth rate.

Yet, those apparently so different mechanisms
 appear to have produced
 such strikingly similar patterns
 of hyperbolic deceleration / acceleration.
 Of course, this point needs further investigations.



Thank you for your attention!